

# A COMBINING GENETIC LEARNING ALGORITHM AND RISK MATRIX MODEL USING IN OPTIMAL PRODUCTION PROGRAM

**Dr Mirjana Misita**

*University of Belgrade, Faculty of Mechanical Engineering, Belgrade, Serbia*

**Dr Galal Senussia \***

*Omar El-Mohktar University, Industrial Engineering Department, El-Baitha, Libya*

**MSc Marija Milovanović**

*University of Belgrade, Faculty of Mechanical Engineering, Belgrade, Serbia*

*One of the important issues for any enterprises is the compromise optimal solution between inverse of multi objective functions. The prediction of the production cost and/or profit per unit of a product and deal with two obverse functions at same time can be extremely difficult, especially if there is a lot of conflict information about production parameters. But the most important is how much risk of this compromise solution. For this reason, the research intrduce and developed a strong and cabable model of genatic algorithm combining with risk management mtrix to increase the quality of decisions as it is based on quantitive indicators, not on qualittive evaluation. Research results show that integration of genetic algorithm and risk management matrix model has strong significant in the decision making where it power and time to make the right decesion and improve the quality of the decision making as well.*

*Key words: Multi-objective function, Genetic Algorithm, Risk Management, Optimum Production Program, Matrix, Costs*

## INTRODUCTION

The analysis of the production program of enterprises is an important and complex segment of managing the enterprise, considering the fact that it influences all elements or resources, such as planning of the material, human resources, machinery resources, research and development, marketing etc. All of these resources influence in multi-criteria optimization of production program. To reduce and improve the decesion making quality, it is important and necessary to evaluate them to minimize the risk of operating losses.

In investigations carried out to date the production program optimization was based on multi-criteria approach using linear functions [01, 09]. Using nonlinear functions in multi-objective optimization enables the application of genetic algorithms and is a step forward in the analysis of the product optimal quantities to maximize production resources utilization [06, 10, 07]. On the other hand, economic calculation of the product cost price is a complex procedure, so that the analysis of optimal production program most

commonly employed direct costs to determine the cost price and to define the cost function. However, cost functions based only on product variable costs cannot provide real optimal product quantities but are more suitable for ranking products that should be given priority in manufacturing. Introducing overhead costs in the function of cost price is a complex calculation procedure most often difficult to understand by the user in a concrete enterprise, considering that it is not easy to classify individual expenses. It is thought that in metalworking companies, roughly assessing, direct costs account for about 60% of total unit costs, while the share of overhead costs is 40% [03].

In business of enterprises, there are several categories of risk: risk of equipment failure (estimated in relation to human safety, to evironment, to business losses, ect.), risk management as a security measure, financial risk assessment in cases of loan approval, quality management risk, ect. Generally, Enterprise Risk Management is relatively new concept, Fraser and Simskins [05] distinguish following risk categories: Shareholder

value risk, Financial reporting risk, Governance risk, Customer and market risk, Operations risk, Innovation risk, Brand risk, Partnering risk, Communications risk.

Risk management consist of strategic risk, operational risk, financial risk and risk acceptance. Strategic risk deal with competition, market position and economic conditions. Operational risk

Concerned with the daily operations, precisely, to the consequences of daily decisions made in the company. The financial risks are related to relations with banks and stockholders, etc. The types of risk and process steps introduced by Risk Management Committee 2003 [11].

Table 1: Enterprise Risk Management [8]

ERM Framework				
Process steps	Type of risk			
	Hazard	Financial	Operational	Strategic
Establish Context				
Identify risk				
Analyze / quantify risks				
Integrate risk				
Assess / Prioritize Risks				
Treat / Exploit Risks				
Monitor & Review				

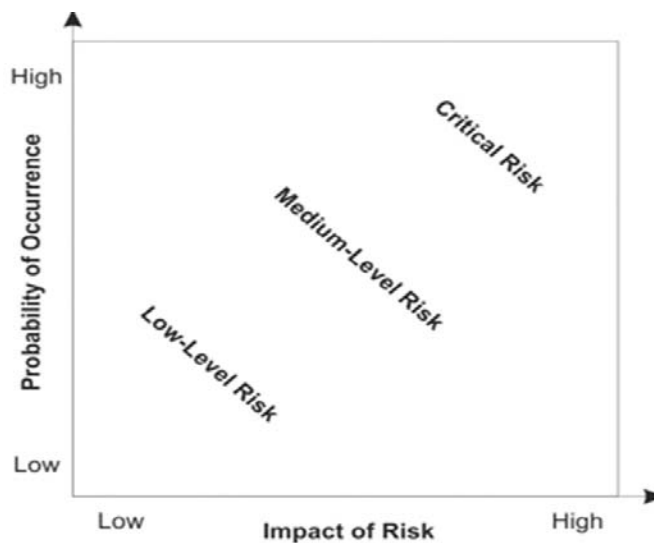


Figure 1: Risk Impact/Probability Chart

The risk is defined as product of probability and consequence of certain events, which can be expressed in formula:

$$R = P \cdot Q$$

P - Probability a particular event.

Q – Consequences of particular event.

For any enterprises, there are external and internal of n-sources of risk. The total risk will represented by high-risk, medium-risk and low-risk sources of operating losses.

$$R_i = \{R_{high}, R_{medium}, R_{low}\}, \quad i = 1, 2, \dots, n$$

The based approach of applying risk are risk identification - what can affect the implementation of production program, risk analysis - defining the probability of occurrence of that, and risk assessment - determining the consequences, expressed in the form of operating losses. The most low-risk sources of operating losses refer to good quality decision. Figure 2 shows the map for identifying Business risks.

Glover at all [9] states that the most real life optimization and scheduling problems are too complex to be solved completely and that the complexity of real life problems often exceeds the

ability of classic methods. Miettinen [08] considered that a key challenge in the real-life design is to simultaneously optimize different objectives through taking into account different criteria low cost, manufacturability, long life and good performance, which cannot be satisfied at the same time.

Profit maximization is the main objective of business enterprises and as such the subject of numerous investigations. Profit is defined as the difference between the total revenue generated by selling products on the market and the overall costs, i.e.:

$$P = TR - TC$$

Where:

- $P$  – Total profit
- $TR$  – Total revenue
- $TC$  – Total cost

When analyzing the possibilities of profit maximization, it is important to consider the fluctuation of the TR and the TC. The TR depends on supply and market demands for particular types of goods, while the TC depends on different constraints faced by the company, such as the mechanical facilities, number and structure of employees, possibility of providing necessary specific materials for the manufacturing process implementation, delivery etc. For the company, to be competitive on the market means to produce a product at an appropriate price and quantity with the use of capital and labor in the appropriate volume and costs. Therefore, profit maximization refers to the optimization of variable parameters in the observed model, with given production constraints.

$$\text{Max } P = \sum_{i=1}^n Q(W_{pi} - W_{vi}) - T_c$$

Where:

- $P$  – Profit
- $Q$  – Quantity of product
- $W_{pi}$  – Selling price of the  $i$ th product
- $W_{vi}$  – Variable cost of the  $i$ th product
- $T_c$  – Constant cost

In real life, the functions of dependence of production quantity and the TR and the TC are nonlinear. The maximum profit is the maximum difference between the total profit curve and the total cost curve, as represented in the Figure 3.

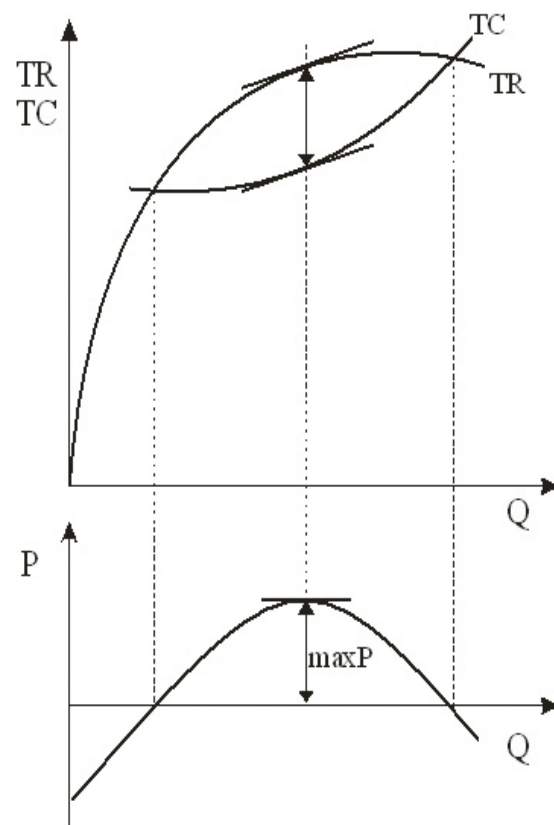


Figure 2: Graphic representation of profit maximization

In real enterprise's operating conditions the functions of the TR and the TC are nonlinear and to determine them two different approaches must be applied.

The TR function consists of the sum of variable and fixed costs, therefore, the sum of linear mathematical form by applying the Lagrange interpolation polynomial based on the values of variable costs from the previous period.

It is possible to determine the nonlinear function of fixed costs in a Lagrange interpolation polynomial is, in our case, a function of production quantity  $P(Q)$  with  $\leq(n-1)$  level if we have  $n$  data points on the value of costs from the previous period.

$$P(Q) = \sum_{j=1}^n P_j(Q)$$

Where:

$$P_j(Q) = y_j \prod_{\substack{k=1 \\ k \neq j}}^n \frac{Q - Q_k}{Q_j - Q_k}$$

## METHODOLOGY

Methodological steps in developing model for risk management integration methodology and GA is shown on Figure 3.

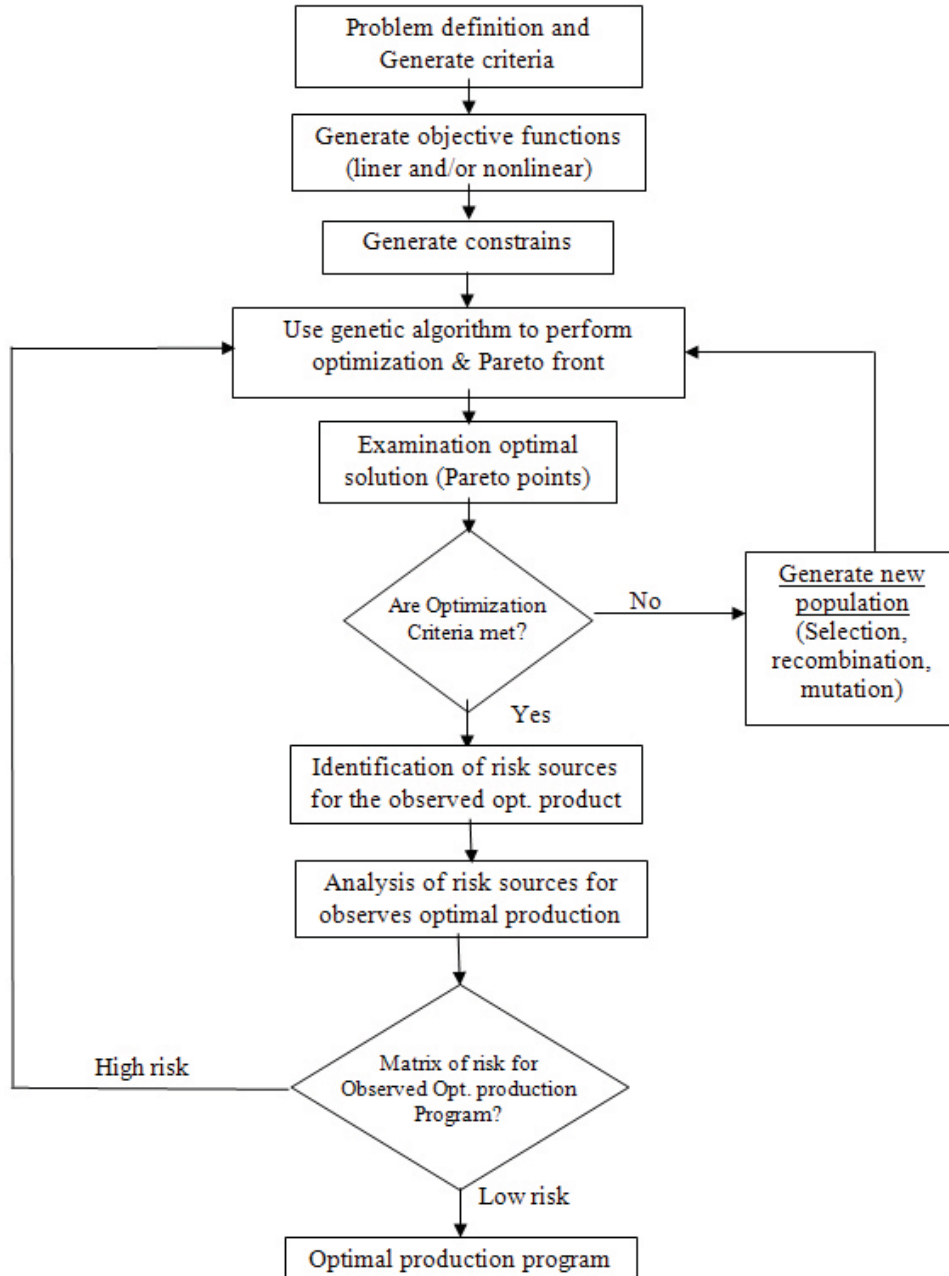


Figure 3: Steps in developing model for risk management integration methodology and GA

## CASE STUDY

In the company engaged in manufacturing precision measuring instruments, we have analyzed the available data and formed nonlinear functions of the TR and the TC for the three products:

a) Clocks

Revenue function:

$$f(x)_{11} = TR(Q) = -0.04Q^2 + 686Q - 1375.3$$

Cost function:

$$f(x)_{21} = TC(Q) = -0.024Q^2 + 410.Q - 4342$$

b) Water meter

Revenue function:

$$f(x)_{12} = TR(Q) = -0.18Q^2 + 4298Q - 343884$$

Cost function:

$$f(x)_{22} = TC(Q) = -0.49Q^2 + 3382.4Q - 463764$$

c) Gas meter

Revenue function:

$$f(x)_{13} = TR(Q) = -0.87Q^2 + 5984.5Q - 5715.1$$

Cost function:

$$f(x)_{23} = TC(Q) = -0.58Q^2 + 3818.2Q - 3643.6$$

The functions of criteria for profit maximization will have the form:

$$\max f(x) = \sum_{i=1}^3 f_{1i} = f(x)_{11} + f(x)_{12} + f(x)_{13}$$

$$\min f(x) = \sum_{i=1}^3 f_{2i} = f(x)_{21} + f(x)_{22} + f(x)_{23}$$

Table 2: Evaluation of risk sources and determination of trend

Risk Source	Risk rating 1 <sup>st</sup> Q. 2010	Risk 2 <sup>nd</sup> Q. 2010	Risk 3 <sup>rd</sup> Q. 2010
Operation cost.	Low	Medium	Medium
Labor cost	Low	Medium	Medium
Lubricant cost	Low	Low	Low
Raw martial cost	Medium	<b>High</b>	<b>High</b>
Fixed cost	Medium	Medium	Medium
capital availability	Medium	Medium	Medium
business operations supply chain management	Medium	Medium	Medium
information technology	Medium	<b>High</b>	<b>High</b>
planning	Medium	Medium	<b>High</b>
reporting	Low	Medium	Medium

Respectively:

$$f(1) = -0.04 \cdot x(1)^2 + 686 \cdot x(1) - 0.18 \cdot x(2)^2 + 4298 \cdot x(2) - 0.87 \cdot x(3)^2 + 5984.5 \cdot x(3) - 350975.4;$$

$$f(2) = -0.024 \cdot x(1)^2 + 410 \cdot x(1) - 0.49 \cdot x(2)^2 + 3382.4 \cdot x(2) - 0.58 \cdot x(3)^2 + 3818.2 \cdot x(3) - 463066;$$

Constraints:

If we consider the production capacity as a key constraint in the production quantity of some products, temporarily ignoring the structure of demand for mentioned products on the market, the restrictions are:

$$0 \leq x_1 \leq 4400$$

$$0 \leq x_2 \leq 2444$$

$$0 \leq x_3 \leq 1100$$

\*\*\*Employees and raw material in the observed company are not of limiting character.

The Pareto front and values of the functions f1 and Figure 1 are shown in Figure 4.

From the Pareto front diagram, it is evident that optimum solution for production quantity and profit maximization under given constraints is a set [2312; 219; 944], where the maximum profit is 5,950,340 RSD calculated as max (f1-f2).

After getting the optimum solution, the second step is Identify and analysis of risk sources for the observed optimum product program. In our case, we have focused on the internal resources only. Identification, evaluations, and determination of trend are shown in the table 2.

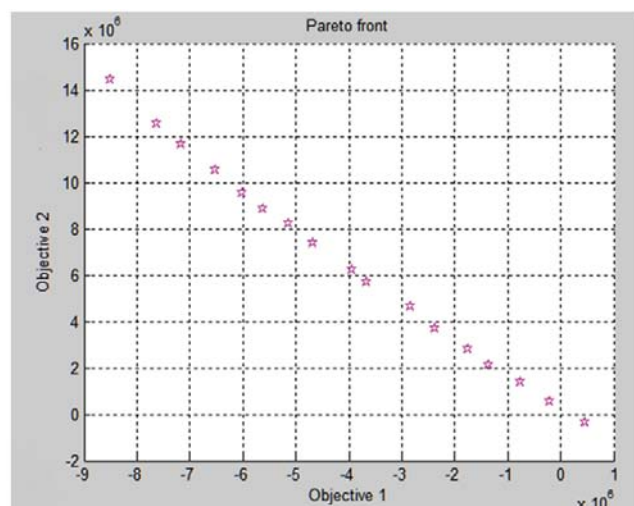


Figure 4: The Pareto front of optimum solution

This figure 5 shows a two-dimension risk map. The vertical axis represents loss likelihood and the horizontal axis represents loss impact. The four quarter panels stand for different combinations of likelihood and impact.

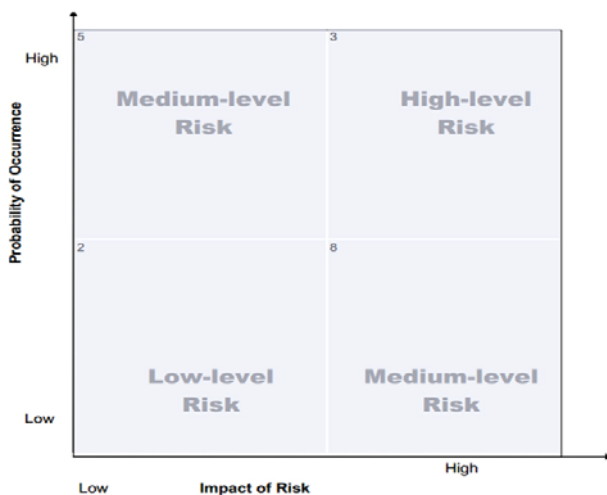


Figure 5: A Two-Dimensional Risk Map

Risk matrix indicates a small number of high-risky, a small number of low-risk risk sources, but the largest number risk sources with medium probability and consequences for business losses, namely:

$$R_i = \{R_{high}, R_{medium}, R_{low}\} = \{2, 15, 3\}$$

Over all research results indicate that at these restrict conditions of production, there is comparatively high risk of production losses. Therefore, it is necessary to resolve our problem to find another optimal solution and repeat analysis until achieved an optimal production program.

## CONCLUSIONS

A strong and capable model of genetic algorithm combining with risk management matrix is introduced and developed to get optimal production program and increase the quality of decisions.

Applying genetic algorithm as a technique deals with huge conflict constraints to create one or alternative optimal solutions. On the other hand, applying risk management matrix for choice of optimal production program reduces the risk of operating losses and affects the efficiency of management. Furthermore, qualitative aspects that are defined through risk sources and by its identification and evaluation, more realistic production program evaluation can be taken into account. Integrated both of them, genetic algorithm and risk management matrix guide to optimal production program.

## REFERENCES

- 1) C. McNair: Defining and Shaping the Future of Cost Management, Journal of Cost Management, Vol. 14, No. 5, 2000, pp. 28-32, ISSN 1092-8057.
- 2) Curović, D., Vasić, B., Popović, V., Curović, N.: Ekspertsko planiranje proizvodnje, (2008) Journal of Applied Engineering Science (Istraživanja i projektovanja u privredi), no. 20, p.49-57
- 3) Eckart, Z., Evolutionary Algorithms for Multi-objective Optimization: Methods and Applications. PhD thesis, Swiss Federal Institute of Technology (ETH), Zurich, Switzerland, November 1999.
- 4) Glover F., Kelly J.P., Laguna M., New Advances for Wedding Optimization and Simulation, Proceedings of the 1999 Winter Simulation Conference, 1999.
- 5) J. Fraser, B.J. Simskins: Enterprise risk management: Today's Leading Research and Best Practices for Tomorrow's Executives, John Wiley & Sons, ISBN 978-0-470-49908-5, USA, 2010.
- 6) J. Sanchis, et al.: A new perspective on multi-objective optimization by enhanced normalized normal constraint method, Structural and Multidisciplinary Optimization, 2008, Vol. 36, No. 5, pp. 537-546, ISSN 1615-1488.
- 7) L. Chi-Ming, G. Mitsuo: An Effective Decision-Based Genetic Algorithm Approach to Multi-objective Portfolio Optimization Problem, Applied Mathematical Sciences, 2007, Vol. 1, No. 5, pp. 201 - 210, ISSN 0066-5452.
- 8) Miettinen, K., Nonlinear multi-objective optimization. Springer, 1999.
- 9) N. Fafandjel, A. Zamarin, M. Hadjina: Shipyard production cost structure optimization model related to product type, International Journal of Production Research, 2010, Vol. 48, No. 5, pp. 1479-1491, ISSN 0020-7543.
- 10) S. Utyuzhnikov, P. Fantini, M. Guenov: A method for generating a well-distributed Pareto set in nonlinear multi-objective optimization, Journal of Computational and Applied Mathematics, 2009, Vol. 223, No. 2, pp. 820-841, ISSN 0377-0427.
- 11) The CAS Enterprise Risk Management Committee: Overview of Enterprise Risk Management, Casualty Actuarial Society Forum, 2003, Pages 99-164, ISSN 1046-6487

Paper sent to revision: 29.08.2012.

Paper ready for publication: 26.09.2012.